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**CINEC CAMPUS
FACULTY OF ENGINEERING & TECHNOLOGY
BACHELOR OF SCIENCE HONOURS IN ENGINEERING**

IS1301 Calculus

In class Test - 1

Time allowed: 2 hours

1st of August 2026

Answer All Questions.

INSTRUCTIONS TO CANDIDATES

- This is a closed book examination.
- Attempt **all questions**.
- Show all stages of your work.
- You should write legibly in black or blue ink.

MATERIALS REQUIRED

- Two eight-page answer booklets
- You may use a scientific calculator. This must not be programmable and may be inspected during the examination.

1. a) Solve each of the following inequalities:

i) $\frac{3x-1}{x-1} > 2$

ii) $\frac{3x^2+2x-1}{x+1} \leq 3x + 1$

b) Solve the following equation:

$$2|x - 1| - |x - 2| = 3.$$

(30 Marks)

2.a) Sketch the locus defined by

$$|z - 2i| = |z - 3 + i|.$$

b) Use De Moivre's theorem to find $(\sqrt{3} + i)^6$.

c) Find all fourth roots of $1 + i$.

(30 Marks)

3. a) i) Find an equation of the parabola with vertex $(0,0)$, axis x axis and passing through $(-1, -4)$.

ii) Find an equation of the ellipse with foci $(3, -2)$, $(5, -2)$ and vertices $(1, -2)$, $(7, -2)$.

iii) Find an equation of the hyperbola with foci $(1,3)$, $(7,3)$ and vertices $(2,3)$, $(6,3)$.

- b) A bridge arch has the shape of a parabola. The arch is 40 m wide and reaches a maximum height of 8m above the road. A truck 3m wide travels along the center of the road. Find the maximum height of the truck that can safely pass under the bridge correct to three significant figures.

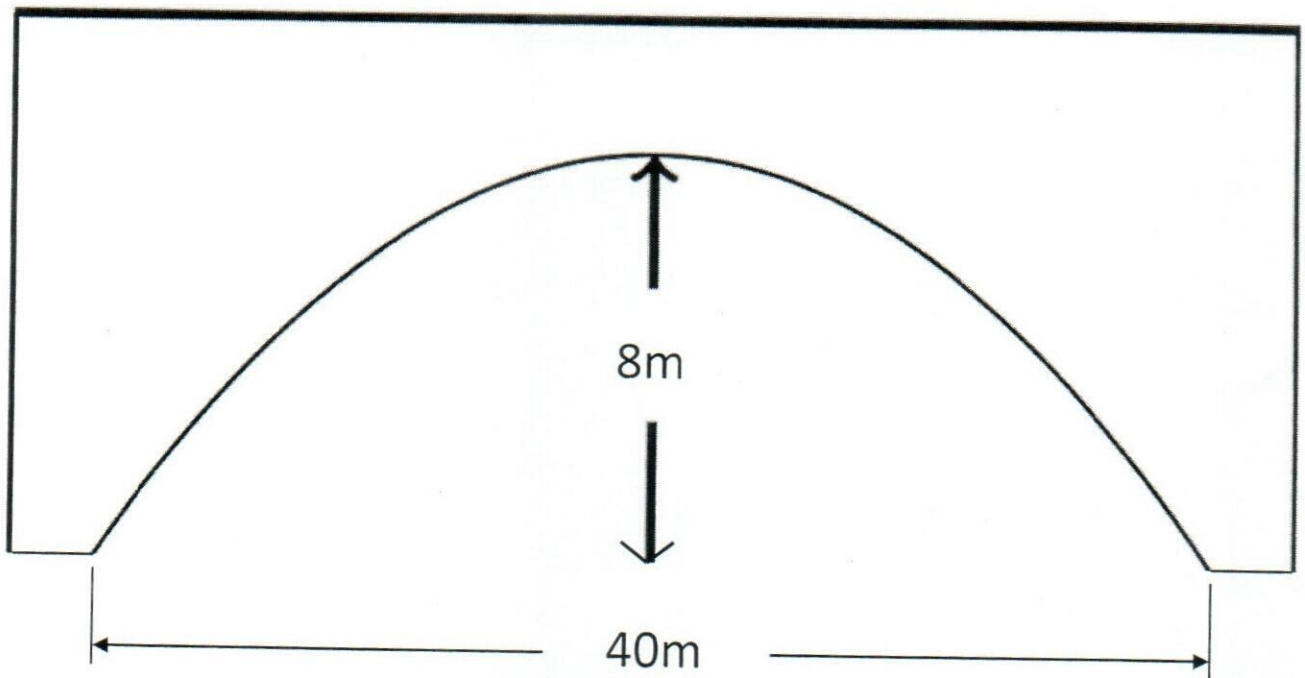


Figure 1

(40 Marks)

Additional Information

n^{th} root formula:

$$\sqrt[n]{r} \left(\cos \frac{\theta + 2\pi k}{n} + i \sin \frac{\theta + 2\pi k}{n} \right) \quad k=0,1,2,\dots,n-1$$

DeMoivre's Theorem

If $z = r(\cos \theta + i \sin \theta)$ is a complex number and n is a positive integer, then

$$\begin{aligned} z^n &= [r(\cos \theta + i \sin \theta)]^n \\ &= r^n (\cos n\theta + i \sin n\theta). \end{aligned}$$