



**MERCHANT SHIPPING SECRETARIAT
GOVERNMENT OF SRI LANKA
CERTIFICATE OF COMPETENCY EXAMINATION**

GRADE : CHIEF MATE ON SHIPS OF 500 GT OR MORE (UNLIMITED)
SUBJECT : SHIP'S STABILITY
DATE : 27.06.2024

Time allowed **THREE hours** Total marks : 180

ANSWER ALL QUESTIONS Pass marks : 60%

Formulae and all intermediate steps taken in reaching your answer should be clearly shown. You may draw sketches wherever required. Electronic devices capable of storing and retrieving are **not** allowed.

- 1) Answer the following questions with regards to bilging:
 - a) "Sometimes the GM will increase after bilging and sometimes it will reduce after bilging". Describe this statement. (05 marks)
 - b) A box shaped vessel of length 100 m and breadth 18 m, floats in salt water on an even keel at 7.5 m draught. The ship has a continuous centre line bulkhead which is watertight. Find the list if a compartment amidships, which is 15 m long and empty, is bilged on one side. Assume the KG is 4 m. (25 marks)
- 2) A vessel completes loading with a displacement of 26000 t and an effective KG of 8.86 m. With the aid of the Hydrostatic particulars and KN curves provided, verify whether the vessel complies with the IMO stability criteria. The progressive flooding angle for the above displacement is 55° . (30 marks)

- 5) Answer the following questions with regards to change of density:
- a) With the aid of a labelled sketch explain why the trim is subjected to change when a vessel moves from one density of water to another.

(05 marks)

- b) A vessel floating in salt water has the following particulars:

Displacement	18,000 t	LBP	220 m
LCB	100 m foap	LCF	120 m foap
MCTC	200	TPC	23
Draft fwd	7.85 m	aft	8.55 m

The vessel has two bunker tanks. The forward tank has its centroid 205 m forward of the aft perpendicular and the after tank has its centroid 75 m forward of the aft perpendicular. Calculate the following;

- i) The amount of fuel to transfer between the bunker tanks in order to arrive alongside at a freshwater berth on an even keel.

(15 marks)

- ii) The arrival draft forward and aft.

(10 marks)

- 6) With reference to a modern shipboard stability and stress finding instruments:

- a) state the hydrostatic and stability data already pre-programmed into the instrument;

(08 marks)

- b) describe the information to be entered into the instrument by the ship's officer;

(10 marks)

- c) describe the output information.

(12 marks)

Draught	Displ.	TPC	MCTC	LCB	LCF	KB	KML	KMT
7.00	21600	32.82	335	86.78	85.53	3.60	265	9.49
7.10	21930	32.88	337	86.76	85.45	3.65	262	9.46
7.20	22260	32.94	339	86.74	85.37	3.70	260	9.44
7.30	22590	33.00	341	86.72	85.28	3.76	258	9.42
7.40	22920	33.07	343	86.70	85.19	3.81	256	9.40
7.50	23250	33.13	345	86.67	85.10	3.86	254	9.39
7.60	23580	33.20	347	86.65	85.01	3.91	252	9.37
7.70	23920	33.27	349	86.63	84.92	3.96	250	9.36
7.80	24250	33.34	351	86.61	84.82	4.02	248	9.35
7.90	24590	33.41	353	86.58	84.72	4.07	246	9.34
8.00	24920	33.48	355	86.55	84.62	4.12	245	9.33
8.10	25250	33.55	357	86.53	84.51	4.17	243	9.32
8.20	25590	33.63	359	86.50	84.40	4.22	242	9.32
8.30	25930	33.71	362	86.47	84.29	4.28	240	9.31
8.40	26270	33.79	365	86.44	84.17	4.33	238	9.31
8.50	26610	33.87	368	86.41	84.05	4.38	237	9.31
8.60	26950	33.95	370	86.38	83.94	4.43	236	9.31
8.70	27290	34.03	373	86.35	83.83	4.48	234	9.32
8.80	27630	34.11	375	86.32	83.72	4.54	233	9.32
8.90	27970	34.19	378	86.29	83.62	4.59	232	9.33
9.00	28310	34.27	381	86.25	83.52	4.64	231	9.34
9.10	28650	34.35	384	86.22	83.41	4.69	230	9.35
9.20	28990	34.43	386	86.19	83.30	4.74	229	9.36
9.30	29340	34.51	389	86.15	83.20	4.80	228	9.37
9.40	29690	34.59	391	86.12	83.10	4.85	227	9.38
9.50	30040	34.67	394	86.09	83.00	4.90	226	9.39
9.60	30390	34.75	396	86.05	82.90	4.96	225	9.40
9.70	30740	34.82	399	86.01	82.80	5.01	224	9.41
9.80	31090	34.89	401	85.97	82.70	5.06	223	9.43
9.90	31440	34.96	404	85.93	82.60	5.11	221	9.44
10.00	31790	35.03	406	85.89	82.50	5.17	220	9.46
10.10	32140	35.10	409	85.86	82.41	5.22	219	9.47
10.20	32490	35.17	411	85.82	82.32	5.27	218	9.49
10.30	32840	35.24	413	85.78	82.24	5.33	217	9.51
10.40	33190	35.31	415	85.74	82.16	5.38	216	9.53
10.50	33540	35.38	418	85.70	82.08	5.44	215	9.55
10.60	33890	35.45	420	85.66	82.00	5.49	214	9.57
10.70	34250	35.52	423	85.62	81.93	5.55	213	9.59
10.80	34610	35.59	425	85.59	81.86	5.60	212	9.61
10.90	34970	35.66	427	85.55	81.79	5.65	211	9.63
11.00	35330	35.72	429	85.51	81.72	5.71	210	9.66

DISPLACEMENT (t)	ANGLE OF HEEL - DEGREES					
	10	20	30	40	60	80
7000	2.97	5.35	6.72	7.55	8.53	8.32
8000	2.75	5.10	6.52	7.47	8.60	8.35
9000	2.56	4.87	6.38	7.40	8.65	8.38
10000	2.39	4.65	6.22	7.34	8.69	8.40
11000	2.25	4.45	6.10	7.28	8.71	8.40
12000	2.13	4.26	5.97	7.24	8.70	8.40
13000	2.03	4.10	5.86	7.20	8.69	8.40
14000	1.94	3.95	5.75	7.16	8.67	8.39
15000	1.88	3.83	5.65	7.14	8.63	8.38
16000	1.82	3.72	5.58	7.10	8.58	8.36
17000	1.78	3.63	5.50	7.05	8.54	8.34
18000	1.74	3.55	5.44	7.01	8.48	8.32
19000	1.70	3.49	5.36	6.96	8.44	8.30
20000	1.69	3.45	5.30	6.90	8.38	8.28
21000	1.66	3.40	5.25	6.85	8.34	8.25
22000	1.65	3.36	5.20	6.80	8.28	8.23
23000	1.65	3.34	5.15	6.72	8.23	8.22
24000	1.64	3.32	5.10	6.65	8.17	8.17
25000	1.64	3.31	5.08	6.58	8.11	8.15
26000	1.64	3.30	5.04	6.50	8.06	8.14
27000	1.64	3.30	5.00	6.44	8.00	8.11
28000	1.65	3.31	4.95	6.36	7.93	8.10
29000	1.65	3.31	4.93	6.30	7.86	8.07
30000	1.65	3.31	4.89	6.22	7.80	8.05
31000	1.65	3.32	4.84	6.14	7.74	8.03
32000	1.66	3.34	4.80	6.06	7.69	8.00
33000	1.66	3.36	4.75	5.99	7.62	7.99

The volumes of buoyancy include poop and forecandle but not hatches.

Answers

Answer 1(a)

Volume of gained buoyancy = Volume of gained buoyancy

$$\begin{aligned} S &= 15 \times 9 \times 7.5 / (100 \times 18 - 15 \times 9) \\ &= 0.61 \text{ m} \end{aligned}$$

$$\text{Bilged draught} = 7.5 + 0.61 \text{ m} = 8.11 \text{ m}$$

$$\begin{aligned} \text{Transverse shift of centre of buoyancy} &= 15 \times 9 \times 4.5 / (100 \times 18 - 15 \times 9) \\ &= 0.37 \text{ m} \end{aligned}$$

$$I_{xx} = (9^3 \times 100 + 9^3 \times 85) / 3 = 44955 \text{ m}^4$$

$$\begin{aligned} I_{yy} &= I_{xx} - Ad^2 = 44955 - (100 \times 18 - 15 \times 9) \times 0.365^2 \\ &= 44733 \text{ m}^4 \end{aligned}$$

$$\begin{aligned} \text{BM} &= I_{yy} / V = 44733 / (100 \times 18 \times 7.5) \\ &= 3.31 \text{ m} \end{aligned}$$

$$\text{KB} = \text{bilged draught} / 2 = 8.11 / 2 = 4.06 \text{ m}$$

$$\text{KM} = \text{KB} + \text{BM} = 4.06 + 3.31 = 7.37 \text{ m}$$

$$\text{GM after bilging} = \text{KM} - \text{KG} = 7.37 - 4.00 = 3.37 \text{ m}$$

$$\begin{aligned} \text{Tan list} &= \text{shift of buoyancy} / \text{bilged GM} \\ &= 0.37 / 3.37 \end{aligned}$$

$$\underline{\underline{\text{List} = 6.3^\circ}}$$

Answer 2

From tables;

$$KM = 9.31 \text{ m}$$

$$GM = KM - KG = 9.31 - 8.86 = 0.45 \text{ m}$$

From KN curves;

Heel	10	20	30	40	60	80
KN	1.64	3.3	5.04	6.5	8.06	8.14
KG x Sin heel	1.54	3.03	4.43	5.7	7.67	8.73
GZ	0.10	0.27	0.61	0.8	0.39	- 0.59

Area up to 30°

Heel	GZ	SM	Product
0	0.00	1	0.0
10	0.10	3	0.3
20	0.27	3	0.81
30	0.61	1	0.61
Total			1.720

$$\text{Area} = 3 \times 10 \times 1.72 / (8 \times 57.3) = 0.113 \text{ m rad}$$

Area up to 40°

Heel	GZ	SM	Product
0	0.00	1	0.0
10	0.10	4	0.4
20	0.27	2	0.54
30	0.61	4	2.44
40	0.8	1	0.8
Total			4.18

$$\text{Area} = 10 \times 4.18 / (3 \times 57.3) = 0.243 \text{ m rad}$$

$$\text{Area between } 30^\circ \text{ and } 40^\circ = 0.243 - 0.113 = 0.13 \text{ m rad}$$

Area between 0 and 30 – Complies

Area between 0 and 40 – Complies

Area between 30 and 40 – Complies

GZ shall be at least 0.2 m – Complies

Maximum righting lever – Complies

Initial GM at least 0.15 m – Complies

Answer 3(a)

$$\text{Max air draught available} = 20.24 - 0.3 = 19.94 \text{ m}$$

$$\text{Max draught under fwd mast} = 25.92 - 19.94 = 5.98 \text{ m}$$

$$\text{Max draught under aft mast} = 26.94 - 19.94 = 7.00 \text{ m}$$

$$\text{Trim between masts} = 26.94 - 25.92 = 1.02 \text{ m}$$

$$\text{Distance between masts} = 112 - 37 = 75 \text{ m}$$

$$\text{Req. draught aft} = 7 + 1.02 \times 37 / 75 = 7.503 \text{ m}$$

$$\text{Req. draught fwd} = 5.98 - 1.02 \times (137.5 - 112) / 75 = 5.633 \text{ m}$$

Answer 3(b)

$$\text{Initial trim} = 6.38 - 5.22 = 1.16 \text{ m}$$

$$\text{Initial TMD} = 6.38 - 1.16 \times 68.57 / 137.5 = 5.802 \text{ m}$$

$$\text{Final trim} = 7.503 - 5.633 = 1.87 \text{ m}$$

$$\text{Final TMD} = 7.503 - 1.87 \times 68.57 / 137.5 = 6.57 \text{ m}$$

$$\text{Req. increase of draught} = 6.57 - 5.802 = 0.768 \text{ m} = 76.8 \text{ cm}$$

$$\text{Ballast to take} = 76.8 \times 23 = 1766.4 \text{ t}$$

Answer 4

Take moments about keel and centreline:

Load	Kg	Moments	Dist. From centre line	Moments about centre line	
				P	S
20000	9.0	180000			
500	12.0	6000	6 (Stbd)		3000
340	4.5	1530	4.5 (Stbd)		1530
200	11.0	2200	6 (Prt)	1200	
150	1.2	180			
21190		189910		1200	4530
					3330

$$KG = 8.962 \text{ m}$$

$$KM = 10.550 \text{ m}$$

$$FSE = 8 \times 15^3 \times 0.9 / (12 \times 21190)$$

$$= 0.096 \text{ m}$$

$$GM \text{ solid} = 1.588 \text{ m}$$

$$GM \text{ fluid} = 1.492$$

$$\text{Tan list} = 3330 / (21190 \times 1.492)$$

$$\text{List} = 6^0 \text{ stbd}$$

Answer 5 (a)

Change of trim will occur depending upon the position of the LCF and LCB. Stern trim will occur if the $LCF > LCB$ and head trim will occur if the $LCF < LCB$. This has to be explained by means of a diagram.

Answer 5 (b) (i)

$$FWA = \text{Displacement} / (40 \times TPC)$$

$$= 18000 / (40 \times 23) = 19.565 \text{ cm} = 0.196 \text{ m}$$

$$TPC_{\text{fresh water}} = 23 \times 1.000 / 1.025 = 22.4$$

$$\begin{aligned} \text{Weight of increased under water volume} &= FWA \times TPC_{\text{less density}} = 19.565 \times 22.4 \\ &= 438.26 \text{ t} \end{aligned}$$

$$\begin{aligned} \text{Trimming moment} &= \text{Weight of increased under water volume} \times (LCB - LCF) \\ &= 438.26 \times (100 - 120) = 8765.2 \text{ tm} \end{aligned}$$

$$MCTC_2 = 200 \times 1.000 / 1.025 = 195.1$$

$$\begin{aligned} \text{COT} &= \text{Trimming moment} / MCTC_2 = 8765.2 / 195.1 = 44.9 \text{ cm} \\ &= 0.449 \text{ m by stern} \end{aligned}$$

$$\begin{aligned} \text{Total trim after arriving into fresh water} &= \text{initial trim} + \text{COT} \\ &= 0.7 \text{ m} + 0.449 = 1.149 \text{ m} \end{aligned}$$

$$\text{Distance between the tanks} = 205 - 75 \text{ m} = 130 \text{ m}$$

$$\text{COT} = \text{trimming moment} / MCTC_2$$

$$100 \times 1.149 = \text{ballast water to transfer to make her even keel} \times 130 / 195.1$$

$$\text{Ballast water to transfer to make her even keel} = 172.4 \text{ t}$$

Answer 5 (b) (ii)

$$\text{COT due to change of density} = 0.449 \text{ m (by stern)}$$

$$T_a \text{ due to change of density} = 0.449 \times 120 / 220 = 0.245 \text{ m}$$

$$T_f \text{ due to change of density} = 0.449 - 0.245 = 0.204 \text{ m}$$

COT required to make her even keel = 1.149 m (by head)

$$T_a \text{ when making her even keel} = 1.149 \times 120 / 220 = 0.627 \text{ m}$$

$$T_f \text{ when making her even keel} = 1.149 - 0.627 = 0.522 \text{ m}$$

	Fwd (m)	Aft (m)
Initial draught	7.85	8.55
Bodily sinkage	+ 0.196	+ 0.196
	8.046	8.746
T_f / T_a	- 0.204	+0.245
Arrival draught at fresh water	7.842	8.991
T_f / T_a (to make her even keel)	+ 0.522	- 0.627
Even keel draughts	8.364	8.364